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Avkhadiev–Becker type p-valence conditions for harmonic mappings of a disc

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Abstract

© 2017, Allerton Press, Inc.We obtain Avkhadiev–Becker type p-valence conditions for locally univalent harmonic mappings defined in the unit disc.

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Keywords

Becker univalence condition, harmonic mapping, multivalence condition

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